## Lesson 6 Supplementary and Complementary Angles

### Greek Letters





Adjacent Angles Angles that share a common side and have the same origin are called <u>adjacent</u> <u>angles</u>. They are side by side. In Figure 1,  $\alpha$  is adjacent to  $\beta$  and  $\delta$ . It is not adjacent to  $\gamma$ . In figure 1 there are four pairs of adjacent angles,  $\alpha$  and  $\beta$ ,  $\beta$  and  $\gamma$ ,  $\gamma$  and  $\delta$ ,  $\delta$  and  $\alpha$ .

In Figure 2 we added points so we can name the rays that form the angles. The common side shared by adjacent angles  $\angle \alpha$  and  $\angle \beta$ , is  $\overrightarrow{VQ}$ .



*Vertical Angles* Notice that  $\angle \gamma$  is opposite  $\angle \alpha$ . Angles that share a common origin and are opposite each other, are called <u>vertical angles</u>. They have the same measure and are congruent.  $\angle \beta$  and  $\angle \delta$  are also vertical angles.

If  $m \angle \beta$  is 115°, then  $m \angle \delta$  is also 115°. If this is true, then do we have enough information to find the  $m \angle \alpha$ ? We know from the information given in Figure 2 that  $\overrightarrow{RT}$  and  $\overrightarrow{QS}$  are lines. Therefore,  $\angle RVT$  is a straight angle and has a measure of 180°. If  $\angle RVQ \ (\angle \beta)$  is 115°, then  $\angle QVT \ (\angle \alpha)$  must be 180° - 115° or 65°. Since  $\angle RVS \ (\angle \gamma)$  is a vertical angle to  $\angle QVT$ , then it also is 65°.

Supplementary Angles Two angles, like  $\angle \alpha$  and  $\angle \beta$ , whose measures add up to 180°, or that make a straight angle (or straight line) are said to be supplementary. In our example they were adjacent to each other, but they don't have to be adjacent to be classified as supplementary angles.



*Complementary Angles* We can observe many relationships in Figure 3.  $\angle 1$  is adjacent to  $\angle 6$  and  $\angle 2$ .  $\angle 3$  and  $\angle 6$  are vertical angles, as are  $\angle 1$  and  $\angle 4$ .  $\angle 6$  and  $\angle 3$  are also right angles since  $\overrightarrow{DF} \perp \overrightarrow{GE}$ . The new concept is in  $\angle DHE$  and  $\angle GHF$ . Both of these are right angles because the lines are perpendicular. Therefore their measures are each 90°. Then  $m\angle 1 + m\angle 2 = 90°$  and  $m\angle 4 + m\angle 5 = 90°$ . Two angles whose measures add up to 90° are called <u>complementary</u> angles. Notice that from what we know about vertical angles,  $\angle 1$  and  $\angle 5$  are also complementary. Let's use some real measures to verify our conclusions.



In Figure 4, let's assume that  $m \angle 1 = 47^{\circ}$ . Then  $m \angle 2$  must be  $43^{\circ}$  since they add up to  $90^{\circ}$ . If  $m \angle 1 = 47^{\circ}$ , then  $m \angle 4$  must also be  $47^{\circ}$  since they are vertical angles, and  $m \angle 5$  must be  $43^{\circ}$ . So  $\angle 1$  and  $\angle 5$  are complementary, as are  $\angle 2$  and  $\angle 4$ . Remember that supplementary and complementary angles do not have to be adjacent to qualify.

It helps me not to get supplementary and complementary angles mixed up by thinking of the "s" in straight and the "s" in supplementary. The "c" in complementary may be like the "c" in corner. For those who use cassettes, a C-90 is a popular tape size.

Use the drawing to fill in the blanks.

- 1)  $\angle AHC$  is adjacent to  $\angle$  and  $\angle$ .
- 2)  $\angle$  BHD is adjacent to  $\angle$  and  $\angle$ .
- 3)  $\angle$  FHB and  $\angle$  are vertical angles.
- 4)  $\angle$  FHC and  $\angle$  are vertical angles.
- 5)  $\angle$  LFJ and  $\angle$  are supplementary angles.
- 6)  $\angle$  FHC and  $\angle$  are complementary angles.
- 7)  $\angle$  JFH and  $\angle$  are supplementary angles.
- 8)  $\angle$  BHD and  $\angle$  are complementary angles.
- 9) If the m $\angle$ CHA = 40°, then m $\angle$ BHD = \_\_\_\_\_.
- 10) If the m $\angle$ JFL = 65°, then m $\angle$ KFH = \_\_\_\_\_.
- 11) If the m $\angle$ FHB = 90°, then m $\angle$ FHA = \_\_\_\_\_.
- 12) If the m $\angle$ CHA = 40°, then m $\angle$ FHC = \_\_\_\_\_.
- 13) If the m $\angle$ LFJ = 65°, then m $\angle$ LFK = \_\_\_\_\_.
- 14) If the m $\angle$ FHB = 90°, then m $\angle$ AHG = \_\_\_\_\_.

### Match each term to the best answer.

- 15) β
- 16) adjacent angles
- 17) supplementary angles
- 18) α
- 19) complementary angles
- 20) vertical angles



Given:  $\overrightarrow{AB}$ ,  $\overrightarrow{CD}$ ,  $\overrightarrow{LG}$  and  $\overrightarrow{JK}$ are straight lines. m∠FHB = 90°.

The drawing is a sketch and not necessarily to scale. Don't make any assumptions about the lines and angles other than what is actually given.

# Sample Student Text Page

- a) share a common ray
- b) alpha
- c) always have the same measure
- d) add up to 90°
- e) add up to 180°
- f) beta

Use the drawing to fill in the blanks.

- 1)  $\angle$  MNS is adjacent to  $\angle$  and  $\angle$ .
- 2)  $\angle$  QNT is adjacent to  $\angle$  and  $\angle$ .
- 3)  $\angle$  SRN and  $\angle$  are vertical angles.
- 4)  $\angle$  MNS and  $\angle$  are vertical angles.
- 5)  $\angle$  QNP and  $\angle$  are supplementary angles.
- 6)  $\angle$ QNT and  $\angle$  are complementary angles.
- 7)  $\angle$ NRZ and  $\angle$  are supplementary angles.
- 8)  $\angle$  MNS and  $\angle$  are complementary angles.
- 9) If the m $\angle$ MNS = 35°, then m $\angle$ SNR = \_\_\_\_\_.
- 10) If the m $\angle$ MNS = 35°, then m $\angle$ TNP = \_\_\_\_\_.
- 11) If the m $\angle$ QNP = 90°, then m $\angle$ PNR = \_\_\_\_\_.
- 12) If the m $\angle$ MSN = 95°, then m $\angle$ NSR = \_\_\_\_\_.
- 13) If the m $\angle$ SRN = 40°, then m $\angle$ YRZ = \_\_\_\_\_.
- 14) If the m $\angle$ XNY = 55°, then m $\angle$ QNT = \_\_\_\_\_.

### Fill in the blanks with the correct terms.

15) The name of the Greek letter  $\alpha$  is \_\_\_\_\_.

- 16) Two angles whose measures add up to 90° are called \_\_\_\_\_\_.
- 17) Two angles whose measures add up to 180° are called \_\_\_\_\_\_.
- 18) The name of the Greek letter  $\gamma$  is \_\_\_\_\_.
- 19) Intersecting lines form two pairs of \_\_\_\_\_\_ angles.

20) The name of the Greek letter  $\delta$  is \_\_\_\_\_\_.



Given: All lines that appear to be straight lines are straight lines.  $m\angle QNP = 90^{\circ}$ .

The drawing is a sketch and not necessarily to scale. Don't make any assumptions about the lines and angles other than what is actually given.

> Sample Student Text Page

Use the drawing to fill in the blanks.

- 1)  $\angle 1$  is adjacent to  $\angle$ \_\_\_\_ and  $\angle$ \_\_\_\_.
- 2)  $\angle 1$  and  $\angle$ \_\_\_\_\_ are vertical angles.
- 3)  $\angle AFE$  and  $\angle \_$  are vertical angles.
- 4)  $\angle$  is a straight angle.
- 5)  $\angle$  is an obtuse angle.
- 6)  $\angle 2$  and  $\angle$ \_\_\_\_\_ are complementary angles.
- 7) If the  $m \angle 2 = 50^{\circ}$ ,  $m \angle 1 =$ \_\_\_\_. Why?
- 8) If the m $\angle 2 = 50^\circ$ , m $\angle 4 =$ \_\_\_\_. Why?
- 9)  $\angle 5$  and  $\angle$  are supplementary angles.
- 10) If the m $\angle 4 = 40^{\circ}$ , then m $\angle 5 =$  \_\_\_\_\_. Why?
- 11) Name two acute angles from the drawing.
- 12) Name two right angles from the drawing.
- 13) Draw a line segment 1 1/2 inches long. Draw its perpendicular bisector using compass and straightedge.



Given:  $\overrightarrow{FC} \perp \overrightarrow{BE}$  $\overrightarrow{DA}$  intersects  $\overrightarrow{BE}$  at F

Remember not to make any assumptions about the lines and angles other than what is actually given.

14) Draw a 52° angle and then bisect it.

Sample Student Text Page

#### Fill in the blanks with the correct terms.

- 15) Two lines forming a right angle are said to be \_\_\_\_\_\_ to each other.
- 16) A right angle has a measure of \_\_\_\_\_°.
- 17) A straight angle has a measure of \_\_\_\_\_°.
- 18) The measures of two complementary angles add up to \_\_\_\_\_°.
- 19) The measures of two supplementary angles add up to \_\_\_\_\_°.
- The intersection of two sets with no elements in common is the \_\_\_\_\_\_ set.

Use the drawing to tell if each statement is true or false.

- 1)  $\angle 2$  and  $\angle 5$  are vertical angles.
- 2) If  $\overrightarrow{FH} \perp \overrightarrow{DK}$ , then  $\angle 2$  and  $\angle 3$  are supplementary.
- 3)  $\angle 3$  and  $\angle 4$  are adjacent angles.
- 4)  $\angle$  FGK is known to be a right angle.
- 5)  $\overrightarrow{GJ}$  is the common side for  $\angle JGK$  and  $\angle KGF$ .
- 6)  $\angle 2$ ,  $\angle 3$  and  $\angle 5$  appear to be acute.

Use the drawing to fill in the blanks.

- 7) If the m $\angle 3 = 39^{\circ}$ , m $\angle 6 =$ \_\_\_\_. Why?
- 8) If  $\overrightarrow{FH} \perp \overrightarrow{DK}$ , and  $m \angle 3 = 39^\circ$ ,  $m \angle 2 =$ \_\_\_\_. Why?
- 9) If  $\overrightarrow{FH} \perp \overrightarrow{DK}$ , then m $\angle 1$  and m $\angle 4$  are each \_\_\_\_\_. Why?
- 10) If the m $\perp$ 1 is 90°, it is a(n) \_\_\_\_\_ angle.
- 11) If the measures of  $\angle 4$  and  $\angle 1$  add up to 180°, they are called \_\_\_\_\_\_ angles.
- 12)  $m \perp 1 + m \perp 2 + m \perp 3 + m \perp 4 + m \perp 5 + m \perp 6 = \____°.$

Match each term to the best answer.

- 13) Greek letter beta
- 14) less than 90°
- 15) measures add to 90°
- 16) Greek letter alpha
- 17) Greek letter gamma
- 18) between 90° and 180°
- 19) measures add to 180°
- 20) Greek letter delta



Given:  $\overrightarrow{DK}$ ,  $\overrightarrow{EJ}$  and  $\overrightarrow{FH}$  intersect at G

Remember not to make any assumptions about the lines and angles other than what is actually given.

Sample

Student Text Page

- b) complementary
- c) δ

a) α

- d) obtuse
- e) acute
- f) β
  - g) γ
    - h) supplementary

Use the drawing to fill in the blanks or answer the questions.

- 1) Name a line containing  $\vec{RV}$ .
- 2) Name a line segment contained in RT.
- 3) If all eight angles were congruent, rather than as given, what would the measure of each be?

Sample

Student Text

Page

- 4) Since the m $\perp$ 1 is 90°, what is m $\perp$ 2 + m $\perp$ 3 + m $\perp$ 4?
- 5)  $\angle 4 + \angle 5$  is a(n) \_\_\_\_\_ angle.
- 6) Are  $\angle 1$  and  $\angle 5$  supplementary?
- 7) Are  $\angle 1$  and  $\angle 5$  complementary?
- 8) Are  $\angle 1$  and  $\angle 5$  vertical angles?
- 9) If  $\angle 2 \cong \angle 3 \cong \angle 4$ , then m $\angle 8 = \__^\circ$ .
- 10) ∠6 ≅ ∠\_\_\_\_
- 11)  $\angle 2$  and  $\angle 3$  are \_\_\_\_\_\_ angles. (size)
- 12) If the m $\angle 2 = 25^\circ$ , and m $\angle 4 = 35^\circ$ , then m $\angle 3 =$ \_\_\_\_\_.
- 13) If the m $\angle 2 = 25^{\circ}$ , and m $\angle 4 = 35^{\circ}$ , then m $\angle YRX =$ \_\_\_\_\_.
- 14) Which ray is the common side for  $\angle$  SRQ and  $\angle$ QRX?
- 15) Draw the perpendicular bisector of the given line segment.





Given:  $\overrightarrow{SW} \perp \overrightarrow{QV}$ All four straight lines intersect at R.

Remember the drawing is a sketch. Use the measurements given in the questions, even if the drawing appears to be different.



Sharpen your algebra skills!

Be very careful when squaring negative numbers.

Example 1:  $(-5)^2 = (-5)(-5) = +25$ Example 2:  $-(8)^2 = -(8)(8) = -64$ Example 3:  $-6^2 = -(6)(6) = -36$ 

17)  $(-7)^2 =$  18)  $-(15)^2 =$  19)  $-12^2 =$  20)  $-(9)^2 =$ 

- Two angles whose measures add up to 180° are called
  - (A) straight (B) complementary (C) acute
  - (D) obtuse (E) supplementary
- 2) Vertical angles are
  - (A) supplementary (B) complementary
  - (C) congruent (D) adjacent (E) obtuse
- 3)  $m \angle XYZ = 35^{\circ}$ . What is the measure of its complement?
  - (A) 145° (B) 55° (C) 35° (D) 65° (E) 125°
- 4) m∠GEF = 40°. What is the measure of its supplement?
  (A) 60° (B) 50° (C) 140° (D) 320° (E) 40°
- 5) Angle A is 20° and angle B is 70°. What is their relationship?
  - (A) supplementary (B) vertical (C) reflexive
  - (D) coplanar (E) complementary

Use this diagram for numbers 6 - 10.



Given:  $\overrightarrow{WT} \perp \overrightarrow{SV}$ ;  $\overrightarrow{RU} \cap \overrightarrow{SV}$  at W.

- 6) ∠1 is adjacent to
  - (A)  $\angle 1$  (B)  $\angle 2$  and  $\angle 5$  (C)  $\angle 3$  (D)  $\angle 4$  (E)  $\angle 2$
- 7) The sum of m∠1 and m∠2 is
  (A) 90° (B) 180° (C) 45° (D) 360°
  (E) can't tell from information given

- 8) The measure of  $\angle UWV$  is
  - (A)  $45^{\circ}$  (B)  $30^{\circ}$  (C)  $90^{\circ}$  (D)  $35^{\circ}$
  - (E) can't tell from information given
- 9) ∠4 and what other angle are vertical angles?
  (A) ∠3 (B) ∠4 (C) ∠2 (D) ∠1
  (E) ∠TWV
- 10) ∠SWT + ∠TWU + ∠UWV =
  (A) 180° (B) 360° (C) 90° (D) 100°
  (E) can't tell from information given





Given: FC, AD, BE intersect at G.

For numbers 11-15, answer:

A if the quantity in column A is greater.

- B if the quantity in column B is greater.
- C if the two quantities are equal.
- D if the relationship cannot be determined from the information given.

	Α	В
11)	m∠2	m∠5
12)	m∠4 + m∠5	136°
13)	180°	m∠2 + m∠3
14)	m∠2	m∠3
15)	185°	measure of 2 right angles

																		I	Practic	e 6A ·	Lesson 6	В
Lesson 6B		are complementary		endicular angles were not in "Given"		s the common side		e vertical angles	re complementary	dicular lines form $90^\circ$ angles		Sample Teacher Manual Page ≩										
	1) True	2) False; they	3) True	4) False; perp listed		5) False; GK i	6) True	7) 39°; they ar	8) 51°; they a	9) 90°; perper	10) right	11) supplement	12) 360	13) f	14) e	15) b	16) a	17) g	18) d	19) h	20) c	
Lesson 6A	1) 2,5	2) 4	3) BFD	4) BFE or AFD	5) BFD or AFC or AFE	6) 1	7) 40°; they are complementary	8) 40°; m $\angle 1$ =40°, $\angle 1$ and $\angle 4$ are vertical angles	<ol> <li>∠1, or ∠4</li> </ol>	10) 140 °; they are supplementary	11) 22, 21, 24	12) Z3; ZCFE	13). I lea a milar to chack. Tha sammant on each	side of the bisector should measure 3/4".	14) The angles on each side of the bisector should measure 26°.	15) perpendicular	16) 90	17) 180	18) 90	19) 180	20) empty or null	
 Practice 6B																						
	1) ∠MNQ, ∠SNR	2) ∠MNQ, ∠TNP	3) ∠YRZ	4) ∠TNP		HNM OF ZPNN	6) ∠TNP	7) ∠YRZ or ∠SRN	8) ∠SNR	9) 55°	10) 35°	11) 90°	12) 85°	13) 40°	14) 55°	15) alpha	16) complementary	17) supplementary	18) gamma	19) vertical	20) delta	
Practice 6A	ZAHG, ZCHF	∠FHB, ∠GHD	ZAHG	ZGHD		ZLFK Or ZJFH	∠CHA	ZHFK or ZJFL	DHG∠	40°	65°	°06	50°	115°	°06			Ø	٩		ũ	
	<del>,</del>	2)	3)	4)	í	(q	(9	4	8)	6	10)	11)	12)	13)	14)	15) 1	16)	17)	18)	19)	20) (	