## **STUDY GUIDES**

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### Fifth Grade Table of Contents

	SOL	Item	Page
1 <sup>st</sup>	5.1	Place Value	
-	5.3	Solve and Estimate	
Six	5.4	Sum and Difference	
Weeks	5.5	Division	
	5.8	Perimeter	
	5.4	Multiplication	
	5.5	Division (continue)	
2 <sup>nd</sup>	5.6	Division of Decimals	
Six	5.3	Multiplication	
	5.8	Area	
Weeks	5.19	Mean, Median, Mode	
	5.20	Patterns (ongoing)	
	5.21	Algebraic Variables (ongoing)	
	5.22	Variables (ongoing)	
3 <sup>rd</sup>	5.2	Order Fractions & Decimals	
Six	5.7	Add and Subtract Fractions	
	5.17	Probability	
Weeks	5.9	Measurement of a Circle	
4 <sup>th</sup>	5.13	Measuring Angles	
-	5.14	Classify Angles	
Six	5.15	Two Dimensional	
Weeks	5.16	Three Dimensional	
1	5.12	Elapse Time	
5 <sup>th</sup>	5.18	Graphs- Stem/Plot	
Six	5.11	Measurement	
Weeks	5.10	Perimeter, Area, Volume	
6 <sup>th</sup>	5.20	Numerical/Geometric Pattern	
Six	5.21	Algebraic Variables	
No. Company and	5.22	Variables	
Weeks	SOL	Test Review	
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# **Probability Study Guide**

Students will solve problems involving the probability of a single event by constructing a sample space and using a tree diagram to identify all possible outcomes of a single event.

Sample space – A list of all the possible outcomes of an activity

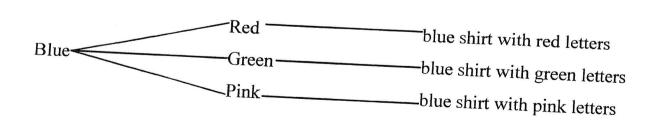
<u>Tree Diagram</u> – A diagram that is commonly used to find the sample space.

### Example:

Our class is ordering T-shirts. The choices are white or blue, and the letters can be red, green, or pink. How many different combinations can be made? Construct a sample space, using a list or chart to represent all possible outcomes.

### Tree Diagram

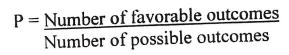
T-shirt	<u>Letters</u>	Outcome
White	Red Green———————————————————————————————————	white shirt with red letters white shirt with green letters white shirt with pink letters



So, there are <u>6</u> possible outcomes.

(You can also multiply the number of T-shirt choices by the number of letter choices)  $2 \times 3 = 6$ 

Students will determine the probability of a single event where the total number of possible outcomes is 12 or less.



**Example1**: Suppose you toss a coin. What is the probability of the coin landing on heads?

$$P(heads) = \frac{Number\ of\ sides\ with\ heads}{Number\ of\ sides} = \frac{1}{2}$$

So there is a 1 out of 2 chance that the coin will land on heads.

You can also say that there is a 50% chance that the coin will land on heads since  $\frac{1}{2} = .50$  or 50%)

Example 2: If you roll a standard die (or number cube), what is the probability it will land on 6?

$$P(6) = \frac{Number\ of\ sides\ with\ a\ 6}{Number\ of\ sides} = \frac{1}{6}$$

So there is a 1 out of 6 chance that the die will land on a 6.

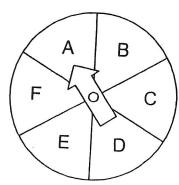
**Example 3:** If you roll a standard die (number cube), what is the probability it will land on a number other than 6?

$$P(not 6) = \frac{Number of sides \ without \ a \ 6}{Number of sides} = \frac{5}{6}$$

So there is a 5 out of 6 chance that the die will not land on a 6.

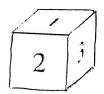
### Sample SOL-style Questions:

1) Shoshanna spins the spinner. What is the probability the spinner will land on a vowel?



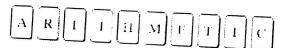
- A. 1 out of 6
- B. 1 out of 5
- C. 2 out of 4
- D. 2 out of 6

2) The sides of a block are numbered 1, 2, 3, 4, 5, and 6. If you toss the block once, what are the chances that the number on top will be a 2 or a 4?



- A. 2 out of 6
- B. 2 out of 4
- C. 2 out of 1
- D. 1 out of 2

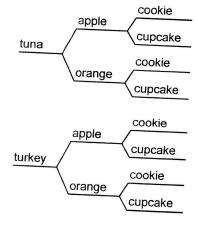
3) Look at the cards below and answer the following question.



Matt picks a card without looking. What is the chance that Matt will draw a T?

- A. 2 out of 8 or  $\frac{2}{8}$
- B. 1 out of 3 or  $\frac{1}{3}$
- C. 2 out of 10 or  $\frac{2}{10}$
- D. 1 out of 8 or  $\frac{1}{8}$

4) According to the tree diagram, how many different ways can you make lunch with 2 sandwich types, 2 types of fruit, and 2 types of dessert?

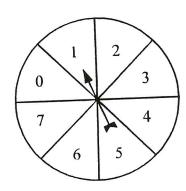


- A. 2 ways
- B. 4 ways
- C. 8 ways
- D. 14 ways

- 5) Luke can either walk or ride the bus to the Y after school. At the Y, he can either swim or play basketball. Which diagram will help you find out how many different ways Luke can get to the Y and choose an activity?
  - A. walk------swim bus-----basketball
  - B. walk——swim——basketball bus——swim—basketball
  - C. walk \_\_\_\_\_\_ swim basketball bus \_\_\_\_\_\_ basketball
  - D. bus swim basketball

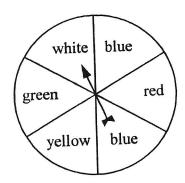
6) Imagine that you spin the spinner below.

The probability of spinning a number greater than zero is \_\_\_\_\_\_



- A. certain.
- B. very likely.
- C. doubtful.
- D. impossible.

7) Out of a total of 20 spins, which color will the spinner probably point to the greatest number of times?



- A. green
- B. yellow
- C. red
- D. blue

- 8) Jerome rolls a number cube labeled 1 to 6. What is the probability that he will roll an even number?
  - A.  $\frac{1}{6}$
  - B.  $\frac{1}{2}$
  - C.  $\frac{2}{3}$
  - D.  $\frac{5}{6}$

# Mean, Median, Mode, Range

SOL 5.19-- The student will find the mean, median, mode, and range of a set of data.

## **Understand:**

Mean, median, mode, and range (MMMR) are four of the various ways that data can be analyzed.

## **Definitions**:

- Mean the AVERAGE of a set of data; found by <u>adding</u> each item of data and <u>dividing</u> by the number of items.
- Median the number that lies in the <u>middle</u> when a set of numbers is arranged in order; if there are two middle values, the median is the mean of these two values.
- Mode the number(s) that occur(s) most often in a set of numbers; there may be one mode, more than one mode, or no mode.
- Range the <u>difference</u> between the greatest number and the least number in a set of data.

# You can find the mean, median, mode, and range for many different types of data and representations of data, including:

- Stem and leaf plots
- Graphs
- Grades/Scores
- Temperatures or other measurements

# HOW TO FIND MEAN

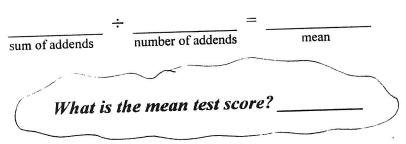
Problem: Students in a math class earned the following scores on their tests:

88, 90, 78, 87, 90, 100, 83, 96

### How to find the MEAN (average):

**Step 1**: Add the scores:  $88 + 90 + 78 + 87 + 90 + 100 + 83 + 96 = ______$ 

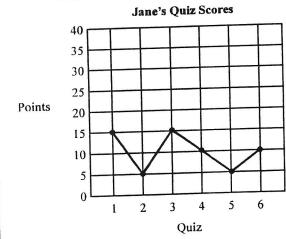
Step 2: Divide the sum by the number of addends (test scores):



### Mean Example 1:

### Mean Example 2:

Look at the graph below and answer the following question.



Find Jane's average quiz score.

- A. 2
- B. 3
- C. 10
- D. 12

What is the mean number of schools in the six towns listed in the chart below?

Number of Schools							
Berkeley 16 Roscoe 14							
Westerly	23	Pottstown	8				
La Estrella	11	Humphrey	12				

- A. 12
- B. 13
- C. 14
- D. 15

# HOW TO FIND MODE

**Problem**: Students in a math class earned the following scores on their tests:

88, 90, 78, 87, 90, 100, 83, 96

### How to find the MODE:

Step 1: Put the numbers in order from least to greatest:

Step 2: Look at the ordered test scores: Is there a number or numbers that occur more often than the rest? That is your mode.

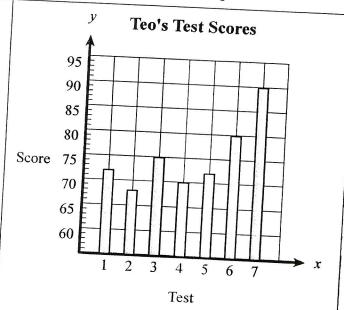
What is mode for this set of test scores?

### **Mode Example 1:**

Tyrell got the following scores on his spelling test: 92, 91, 91, 90, 88, 86, 85, 92, 83, 91. What is the mode of Tyrell's scores?

- A. 92
- B. 91
- C. 90
- D. 88

### **Mode Example 2:**



### What is the mode for the data?

- A. 75
- B. 90
- C. 72
- D. 68

# HOW TO FIND MEDIAN

Problem: Students in a math class earned the following scores on their tests:



88, 90, 78, 87, 90, 100, 83, 96

### How to find the MEDIAN:

Step 1:	Put the numbers in order from least to greatest.
	,,,,,,,
Y	Find the number(s) in the middle: and nt: If you have an even number of values, you will have 2 numbers in the middle. In that case, find the mean of those two numbers. That will be your median.

Step 3: Because there are two numbers in the middle, you will need to find the mean of those two numbers.

number l num	mber 2 sum	THENsum of two	o numbers	(2) median
Wh	nat is the medi	ian for this set of	test scores? _	

Median Example 1:

### Median Example 2:

Number of Puppies Born						
D	Number of					
Dog	Puppies					
Taffy	6					
Princess	9					
Bess	3					
Roxy	5					
Pinky	8					
Lassie	4					
Penny	10					

What is the median number of puppies for the data collected?

A. 3

B. 5

C. 6

D. 7

Rashon takes a 10-word spelling test every Friday. His last six scores were as follows: 88, 92, 25, 40, 60, 80. What was Rashon's median score?

A. 40

B. 60

C. 70

D. 80



# HOW TO FIND RANGE

**Problem**: Students in a math class earned the following scores on their tests:

88, 90, 78, 87, 90, 100, 83, 96

## How to find the RANGE:

\*\*\*Step 1: Put the numbers in order form least to greatest.

\*\*\*Step 2: Find the greatest number:

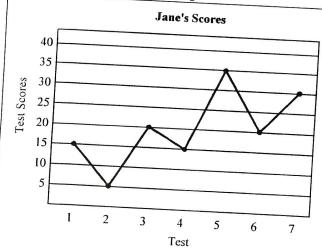
\*\*\*Step 3: Find the lowest number:

\*\*\*Step 4: Find the difference between the greatest and the lowest number:

-	- =	=
greatest number	lowest number	range

What is the range for this set of test scores?

Range Example 1:



What is the range of Jane's test scores?

- A. 10 points
- B. 15 points
- C. 25 points
- D. 30 points

Range Example 2:

The list shows the lengths of six fish caught in the lake. What is the range in the lengths of the fish?

13 in.; 7.5 in.; 9 in.; 11.5 in.; 9.5 in.: 11 in.

- A. 9 in.
- B. 7.5 in.
- C. 5.5 in.
- D. 5 in.

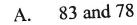
### MIXED EXAMPLES

1) The Lee family traveled from San Francisco to Los Angeles. They covered 300 miles on the first day, 250 miles on the second day, and 200 miles on the third day. What was the mean distance traveled by the Lee family?

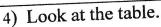


- 250 B.
- 300 C.
- 350 D.

2) David scored 89, 92, 78, 83, 83, and 87 in six tests. List the median and mode for David's scores.



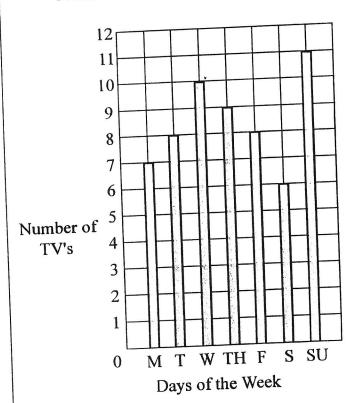
- 85 and 83 B.
- 86 and 83 . C.
  - 87 and 83 D.



# **Test Scores**

Student	Test Score
Arial	88
Martin	84
Tisha	86
Aston	88
Sarah	72

3) Number of TV's Sold in a Week



List the median and mode for the given data.

- 8 and 9 A.
- 9 and 10 B.
- 6 and 10 C.
- 8 and 8 D.

Which student's score is the median and what is the mode of the test scores?

- Arial, 72 A.
- Aston, 84 B.
- Tisha, 88 C.
- Sarah, 88 D.

5) Which statement about the list of numbers is true?

26, 33, 24, 47, 28, 25, 33

6) Jenna scored 10, 20, 15, 25, and 10 points in five basketball games. Find the median and mode of Jenna's scores.

A) The mode and the mean are the same.

- B) The mean and the median are the same.
- C) The mode and the median are the same.
- D) The mode, median, and mean all are different.
- A. 10 and 10

B. 15 and 10

- C. 20 and 10
- D. 25 and 10

7) The fourth-grade classes held a canned food drive. The chart below shows the number of cans collected by each class.

Fourth-Grade Classes	Number of Cans Collected
Ms. Easler	95
Mr. Ketcham	111
Mrs. Mullens	143
Miss Pankow	108
Mr. Turner	153

8) Which set of numbers has a mean equal to its median?

A. 5, 1, 1, 1, 5

B. 2, 2, 3, 2, 2

C. 1, 3, 6, 9, 12

D. 1, 2, 3, 4, 5

What was the mean number of cans collected by the five classes?

A. 111

B. 122

C. 129

D. 153

### Use the stem and leaf plot below to answer questions 9 - 12.

### **Number of Birds**

STEM	LEAF						
0	2	6					
1	2	6	7	9			
2	2	3	5	7	9		

Key: 1/6 = 16

9.	What	is	the	mean?	
----	------	----	-----	-------	--

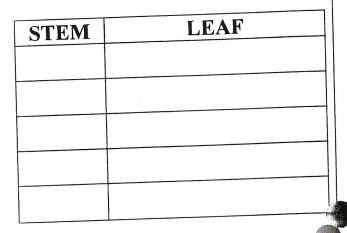
10. What is the range?

11. What is the median?

12. What is the mode?

Create a stem and leaf plot for the following data.

Test Scores								
76	54	92	88	76	88	75	93	92
68	88	76	76	88	80	70	88	72



Use the stem and leaf plot you made above to answer the following questions.

13. What is the median?

14. What is the mean?

15. What is the mode?

16. What is the range?

# Variables and Variable Expressions

SOL 5.21-- The student will investigate and describe the concept of a variable and use a variable expression to represent a given verbal expression involving one operation

## **Understand:**

• A variable is a symbol that can stand for any number

Example: in x + 5, x is a variable

• A <u>variable expression</u> is a variable or combination of variables (x, z, n), numbers (1,2,3), and symbols  $( \square )$  that represents a mathematical relationship.

Examples: 29 + x

412 -

20*m* 

# Parts of an algebraic expression: number, variable, and operation

The variable represents what you do not know.

 $3 \times n$ 

6 - x

Number \_\_\_\_\_

Number\_\_\_\_

Variable \_\_\_\_\_

Variable \_\_\_\_\_

Operation\_\_\_\_

Operation\_\_\_\_

# Using a variable to represent a verbal expression

Create a variable expression for each verbal expression below. Use the variable m to represent what you do not know.

	1			1
-			1 2	
1				
	1		9 /	
			髓	-
		200		

Verbal Expression	Variable expression
Seven plus a number	
A number minus 6	
Thirty-two minus a number	
A number divided by 34	or
17 times a number	or

Write a verbal expression for each algebraic expression below

<u>Vari</u>	able expression	Verbal Expression
	z ÷ 407	
	402 + n	
	450 <i>y</i>	
	n - 32	
7	28 × n	
	32 x	

1) Translate.

eight less than some number

- A. 8 < x
- B. x > 8
- C. 8-x
- D. x-8

2) Translate.

- A. x-7
- B. 7x
- C. x+7
- D. 7-x

3) Translate this expression.

the product of fifteen and n

- A. 15n
- B. 15 + n
- C. 15 n
- D.  $15 \div n$

4) Twelve increased by four can be written as

the sum of seven and some number

- A.  $12 \div 4$ .
- B. 12 + 4.
- C. 12-4.
- D.  $12 \times 4$ .

5) The difference between twelve and some number can be written as

- A. 12 n
- B. 12-9
- C.  $12 \times n$
- D. n + 12

6) Which is the correct phrase for the expression n-11?

- A. a number subtracted from 11
- B. 11 subtracted from a number
- C. a number is less than 11
- D. a number decreased 11 times

7) Which is the variable expression for

### Twice a number



B) 
$$2 - n$$

- C) 2n
- D)  $2 \div n$

8) Which could be the verbal expression for

$$m \div 2$$

- A) The product of a number and two
- B) Twice a number
- C) The difference of a number and two
- D) Half a number
- 9) Which could be the verbal expression for

$$7 + y$$

- A) The difference of seven and a number
- B) The product of seven and a number
- C) Seven more than a number
- D) Seven less than a number

10) Three more than the quotient of four divided by two can be written as

A. 
$$4 + 2 \div 3$$
.

B. 
$$4 \div 2 + 3$$
.

C. 
$$4-2+3$$
.

D. 
$$3 \div 4 + 2$$

- 11) Which is the correct phrase for the expression 3n 11?
- A. three times a number subtracted from 11
- B. eleven less than three times a number
- C. three times a number is less than 11
- D. three times a number less than 11

- 12) Which phrase describes  $\frac{7}{2n}$ ?
  - A. seven times a number divided by 2
  - B. twice a number divided by 7
  - C. 7 divided by twice a number
  - D. 2 divided by 7 times a number

# Variable Expressions & Word Problems

SOL 5.21-- The student will write a variable expression to represent a given mathematical relationship and word problem, using a variable

When writing an algebraic expression for a word problem, you use a variable to represent the value(s) that are unknown.

Chris has \$20 XX	1:
Chris has \$28. He earns an unknown amount of d What expression would show this?	lollars by doing choras
What expression would show this?	tioning chores.
Value you do know Operation	Vonishi
Variable expression of problem:	
The fifth grade unit 1	
The fifth grade raised an unknown amount of money equal amount. If there are five classes in the fifth grade are	for a field trip. Each along
equal amount. If there are five classes in the fifth gramuch each class earned?	ade, what expression would be
much each class earned?	now how how
Value you know Operation	
	Variable
Variable expression:	or
Tamar is going to hake the sample 3:	
Tamar is going to bake the same number of cupcakes expression would show his plan?	each day for the next 14 days. What
and the mas plan!	
7-1	
alue you know Operation	Variable
ariable expression:	
pression.	

### Example 4:

Raina bought an item at the grocery store using a coupon. The original price of the item was \$8.00. The coupon reduced the price. What expression would show this?

	1		1	Y
-		7	V	
	6		Y	
	4			

Value you know \_\_\_\_\_ Operation \_\_\_\_ Variable \_\_\_\_

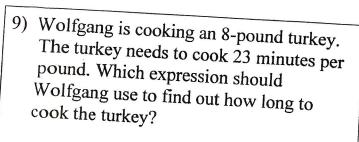
Variable expression:

- 5) Sean washes cars to earn enough money to buy a computer. He charges \$4.50 to wash a car. The computer costs \$800. Which expression will help find the number of cars Sean must wash before he can buy the computer?
- A.  $$800 \div $4.50$
- B.  $$800 \times $4.50$
- C. \$800 \$4.50
- D. \$800 + \$4.50
- 7) Dane gets 5¢ back for every empty soda bottle he recycles. Let b represent the cost of a bottle of soda. After recycling a bottle, which expression below could be used to show how much Dane paid
  - A. b-5

for one soda?

- B.  $b \div 5$
- C. 5-b
- D.  $5 \div b$

- 6) Members of the soccer team held a car wash to raise money for new team uniforms. They charged \$5 for each car they washed. Let *m* represent the total amount of money raised at the car wash. Which expression could be used to find out how many cars the soccer team washed?
  - A. m + 5
  - B. m-5
  - C.  $m \times 5$
  - D.  $m \div 5$
  - 8) Which problem would you use subtraction to solve?
    - A. Kerrie has 13 fish and 2 cats for pets. How many pets does Kerrie have all together?
    - B. 37 books were on the shelf. 7 books were on the table. How many more books were on the shelf than on the table?
    - C. Jin Soo sold 56 tickets. His brother sold 98 tickets. How many tickets did they sell in all?
    - D. 24 baby monkeys were in the zoo. 15 mother monkeys were in the zoo. How many monkeys were in the zoo?



A. 
$$23 + 8$$

B. 
$$23 - 8$$

C. 
$$23 \times 8$$

D. 
$$23 \div 8$$

11) A nursery school had 100 students and 4 teachers. The school calculated the number of students in each class as  $\frac{100}{4} = 25$ .

Which of the problems below can be solved in the same way?

- A. A teacher gave away 4 gifts each to a group of 100 kids. How many gifts did he give away?
- B. Bruce had 100 toys. He received 4 more toys. How many toys did he have in all?
- C. A zoo had 100 animals last year. This year, the zoo has 4 times more animals. How many animals does the zoo have now?
- D. A group of 100 students played a game. Four teams were formed. How many members did each team have?

10) Out of the 25 students who went to football tryouts, only 11 were selected. The number of students who were not selected was calculated as 25 - 11 = 14.

Which of the problems below <u>cannot</u> be solved the same way?

- A. At the final tryout, 25 students appeared. Of those, 11 failed. How many students passed?
- B. Lisa had \$25 with her before shopping. When she went home, she had \$11. How many dollars did she spend?
- C. A company had 25 computers. They purchased 11 more. How many did they have in all?
- D. John had 25 T-shirts. He gave some of these to his friend. John had 11 T-shirts left. How many did he give away?
- 12) Lisa had 30 cookies. She gave a certain number of cookies to her brother. She wanted to figure out how many cookies were left.

Which expression below would help her find the answer?

A. 
$$k - 30$$

B. 
$$k + 30$$

C. 
$$30 \div k$$

D. 
$$30 - k$$

- 13) Merv is three times older than his younger brother. What expression would show how old Merv is?
  - A) m+3
  - B) m-3
  - C)  $m \times 3$
  - D)  $m \div 3$

- 14)Terrence read a certain number of AR books last year. His younger brother Sid read one-half as many books as Terrence did. Which expression would show how many books Sid read?
  - A) t-2
  - B) 2 t
  - C)  $t \times 2$
  - D)  $t \div 2$

- 15) Richard received a certain amount of money for his birthday. Christa received twice as much as Richard did on her birthday. What expression would show how much Christa received?
  - A)  $r \div 2$
  - B)  $r \times 2$
  - C)  $2 \div 10$
  - D)  $r \times 10$

- 16)Clarence went to a clearance sale and bought a new motorcycle for one-fourth the original price. Which expression would show how much he paid for the motorcycle?
  - A) m+4
  - B) m-4
  - C)  $m \times 4$
  - D)  $m \div 4$

# Solving Open Sentences

Addition – Use the inverse operation (subtraction) to solve if needed.

$$4 + n = 7$$
 (Subtract 4 from 7 to get answer)

$$x + 3 = 5$$

$$9 + 5 = z$$

$$n =$$

$$x =$$

$$z =$$

Subtraction -- Use the inverse operation (addition) to solve if needed. If the variable comes immediately after the minus sign, you will need to find the difference of the other two numbers.

$$n - 8 = 8$$
 (Add 8 to 8 to get answer)

$$12 - x = 9$$
(Subtract 12 - 9 to get answer)

$$15 - 5 = z$$

Multiplication -- Use the inverse operation (division) to solve if needed.

$$n \times 3 = 12$$
 (Divide 12 by 3 to get answer)

$$7n = 49$$

$$5 \times 5 = z$$

$$n =$$

$$n =$$

$$z =$$

Division -- Use the inverse operation (multiplication) to solve if needed.

$$k \div 3 = 7$$

(multiply 7 by 3 to get answer)

$$42 \div n = 6$$

$$\frac{32}{z} = 4 \qquad \frac{x}{5} = 60$$

$$\frac{x}{5} = 60$$

$$z =$$
\_\_\_\_  $x =$ \_\_\_

1) Find the missing number.

$$8 + n = 16$$

A. 
$$n = 24$$

B. 
$$n = 12$$

C. 
$$n = 10$$

D. 
$$n = 8$$

2) What is the missing number?

$$13 - b = 6$$

A. 
$$b = 8$$

B. 
$$b = 7$$

C. 
$$b = 19$$

D. 
$$b = 21$$

3) Solve for n.

$$n + 47 = 72$$

A. 
$$n = 17$$

B. 
$$n = 25$$

C. 
$$n = 35$$

D. 
$$n = 129$$

4) Find the value of n.

$$2 \times n = 140$$

A. 
$$n = 60$$

B. 
$$n = 70$$

C. 
$$n = 142$$

D. 
$$n = 280$$

5) What is the value of k?

$$k \div 3 = 12$$

A. 
$$k=4$$

B. 
$$k = 9$$

C. 
$$k = 15$$

D. 
$$k = 36$$

6) What number makes the following sentence true?

$$n - 6 = 17$$

A. 
$$n = 11$$

B. 
$$n = 12$$

C. 
$$n = 23$$

D. 
$$n = 24$$

# Open Sentences & Word Problems

Open sentence – a mathematical sentence containing a variable and an equals (=) sign.

Example: 4 + x = 7

<b>Exam</b>	pl	e	1	
794.754 - 55000		_	_	

(Hint: Highlight your known values and identify what the variable represents)

Tam writes four letters each day. How many letters does he write in 8 days?

Operation Variable = m

Open sentence \_\_\_\_

m =\_\_\_\_\_letters

### Example 2:

A certain number of pencils are in a box at a store. Three pencils are

Operation Variable = p

Open sentence

*p* = \_\_\_\_\_

### Example 3:

Stan baked 24 cupcakes and divided them into an unknown number of containers. There are 6 cupcakes in each container. How many containers are there?

Operation\_\_\_\_

Variable = C

Open sentence \_\_\_\_\_

c =\_\_\_\_\_ containers

### Example 4:

Samantha spends 35 minutes reading every day. Which equation shows how much time she spends reading in a week?

A) 
$$35 \div 7 = y$$

B) 
$$35 + 7 = y$$

 $y = \underline{\hspace{1cm}}$  minutes

C) 
$$35 \times 7 = y$$

D) 
$$35 - 7 = y$$

#### Example 5:

Tamara ran 58 laps on Saturday. She ran 24 laps in the morning. Which equation below shows how many laps she ran in the afternoon?

A) 
$$58 + 24 = x$$

B) 
$$58 + x = 24$$

C) 
$$58 \div x = 24$$

$$x = \underline{\hspace{1cm}}$$
 minutes

D) 58 - x = 24

6) Out of the 25 students who went to football tryouts, only 11 were selected. The number of students who were not selected was calculated as 25 – 11 = 14.

Which of the problems below <u>cannot</u> be solved the same way?

- A. At the final tryout, 25 students appeared. Of those, 11 failed. How many students passed?
- B. Lisa had \$25 with her before shopping. When she went home, she had \$11. How many dollars did she spend?
- C. A company had 25 computers. They purchased 11 more. How many did they have in all?
- D. John had 25 T-shirts. He gave some of these to his friend. John had 11 T-shirts left. How many did he give away?

7) There are 10 pounds of oranges in each of 5 bags. How many pounds of oranges are there in all?

Which number sentence tells you how to find the answer to this problem?

A. 
$$10 - 5 = n$$

B. 
$$10 + 5 = n$$

C. 
$$10 \times 5 = n$$

D. 
$$10 \div 5 = n$$

8) Ryan has 60 pens, 20 of which are black. The rest of his pens are blue. Which number sentence could be used to find the number of Ryan's pens that are blue?

A. 
$$50 + 20 = b$$

B. 
$$b - 20 = 60$$

C. 
$$60 - 20 = b$$

D. 
$$60 + 20 = b$$

Eighty people attended the spaghetti dinner in the cafeteria at Villa Point Elementary School. They sat at 20 tables with the same number of people at each table. How many people sat at each of the tables?

Which number sentence would help you to solve the problem in the box above?

A. 
$$80 - 20 = n$$

B. 
$$80 \times 20 = n$$

C. 
$$80 + 20 = n$$

D. 
$$80 \div 20 = n$$

### 10)

Darla had 48 coins. She divided them evenly into piles. She made 6 piles in all. Find s, if s equals the number of coins in each pile.

A) 
$$48 \times s = 6$$

B) 
$$48 \div s = 6$$

C) 
$$48 + s = 6$$

D) 
$$48 - s = 6$$

### 11)

Dan bought 3 tickets to a show. He paid \$24 in all. How much did each ticket cost, if the cost of a single ticket = m?

A) 
$$3 + m = 24$$

B) 
$$3 - m = 24$$

C) 
$$3 \div m = 24$$

D) 
$$3 \times m = 24$$

### 12)

Which of these could be solved using the open sentence a - 4 = 32?

- A) Kiana had 32 pieces of candy. She divided the candy into 4 equal piles. How many pieces of candy were in each pile?
- B) Joseph is 4 times older than his baby brother. If Joseph is 32 years old, how old is his baby brother?
- C) Crystal earned \$32 babysitting one Friday. She then earned \$4 more by doing chores on Saturday. How much money did Crystal earn altogether?
- D) Heather received money for her birthday, and then spent \$4 of it at the store. She had \$32 left. How much money did Heather receive for her birthday?

### 13)

Which can be solved by using the open sentence k + 5 = ?

- A) John did 5 times as many sit-ups as Kurt.

  If *k* is the number of sit-ups Kurt did, how many sit-ups did John do?
- B) Reba ran 5 fewer meters than Sharon. If k is the number of meters that Sharon ran, how many meters did Reba run?
- C) Shaquan takes 5 minutes to run each lap around the football field. If *k* is the number of laps Shaquan ran, how long did he run?
- D) Briana did 5 more push-ups than Karen. If k is the number of push-ups that Karen did, how many pushups did Briana do?

# **Patterns**

## **Repeating Patterns**

These are the simplest types of patterns. You only need to figure out the "core" or basic unit, and then repeat it.

### **Examples:**

- 1) AABBCCAABBCCAABB \_\_\_\_ (Core: \_\_\_\_\_)
- 3) Tamisha strung beads to make a necklace. The picture shows the pattern.



What will the fifteenth bead look like?

- A. black
- B. white
- C. striped
- D. green

4) Look at the pattern below.

ABCCDABCCDAB

What will be the twentieth letter in the pattern shown above?

- F. A
- G. B
- H. C
- J. D

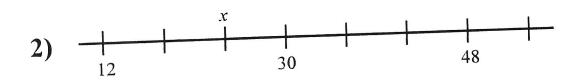
## **Growing Patterns**

These are a little harder. You have to figure out the "rule", or what is happening to the part of the pattern you can see. Sometimes you also have to figure out what comes next or fill in missing pieces of the pattern.

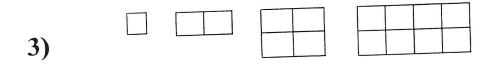


### Examples:

1) 6, 9, 12, 15, 18, \_\_\_\_, (Rule: \_\_\_\_)



What number is x? \_\_\_\_\_ What is the rule? \_\_\_\_\_



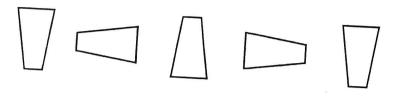
What is the rule? \_\_\_\_\_

4) 2.10, 2.13, \_\_\_\_\_, 2.22, \_\_\_\_\_, \_\_\_\_

What is the rule? \_\_\_\_\_

## Geometric Patterns

These usually involve a figure that changes in some way, usually by rotating (turning) or



Draw the next figure

What is the rule?

5) During a math contest, Paul got 5 correct answers on the first day. On the second day, he got 8 correct. The third day he got 13 correct, and the fourth day he got 20 correct. If this pattern continues, how many correct answers will Paul get on the fifth day?

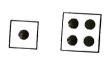
C. 25

6) What will be the 5th term in the pattern below?

- Α. 10
- B. 13
- C. 14
- D. 17
- 7) How many dots will be in the next box?

B. 23

8) Five students board a bus at the first stop, 7 at the second, 10 at the third, and 14 at the fourth. How many students board the bus at the fifth stop?



A. 21





D. 29

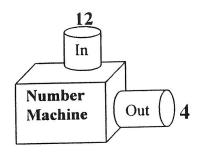
- A.5B. 20
- C. 25 D. 36
- A. 17 B. 18 C. 19
  - - D. 20

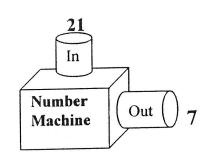
## **Function Machines/Tables**

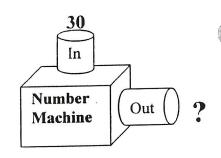
(also called Number Machines)

These are "math machines" where you put in a number and a (usually different) number comes out. There is a rule that the machine is using to change the numbers. Sometimes you have to find out the rule the machine is using, and sometimes you have to use the given rule to find missing numbers. The "machines" can look very different, but they all work in the same way.

#### **EXAMPLE 1:**

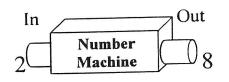


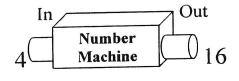


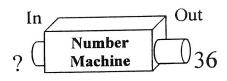


Rule:

#### **EXAMPLE 2:**







Rule:\_\_\_\_\_

### **EXAMPLE 3:**

Rule:		
Input	Output	
4	8	
6	12	
8		

### **EXAMPLE 4:**

Rule:				
Input	Output			
34	59			
х	70			
52	77			
66	У			

5) Look at the table below.

x	1	3	5	7
y	11	33		

## Identify the function of the table:

A. 
$$y = x + 11$$

B. 
$$y = x + 0.11$$

C. 
$$y = 11x$$

D. 
$$y = x - 11$$

6) Rakim is ordering new chairs for his office. A chart in the catalog gives him the weight of the chairs.

Number of Chairs	2	3	4	5
Total Weight	16	24	32	40

If the pattern continues, what would be the total weight of 8 chairs?

Answer:	

Rule:

7) What three numbers should come next in the sequence?

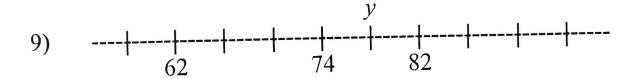
# 1, 2, 4, 7, 11, 16, 22, ...

- A. 27, 32, 40
- B. 28, 35, 43
- C. 29, 37, 46
- D. 30, 38, 47

8) Which statement about this pattern is true?

5, 11, 17, 23, ...

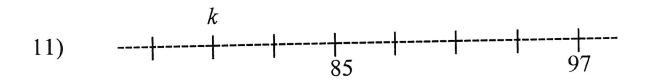
- **A.** Each number is 6 more than the number to its right.
- **B.** Each number is 2 times the number before it.
- C. Each number is the second odd number after the number before it.
- **D.** Each number is 6 less than the number to its right.



y =\_\_\_\_\_\_Rule: \_\_\_\_\_

$$m =$$

m =\_\_\_\_\_ Rule: \_\_\_\_\_



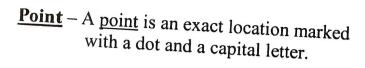
$$k =$$

 $k = \underline{\hspace{1cm}}$  Rule:  $\underline{\hspace{1cm}}$ 

$$x =$$

x =\_\_\_\_\_\_Rule: \_\_\_\_\_

# Lines





 $\underline{\mathbf{Ray}} - \mathbf{A} \underline{\mathbf{ray}}$  is a line that has an endpoint and extends on forever in one direction



Line - A line is a straight path of points that never ends and goes on forever in two directions.

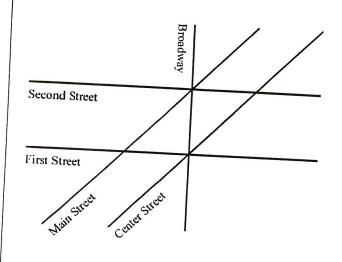


# **Types of Lines**

Туре	Example	Definition
Vertical Line		A <b>vertical</b> line goes straight up and down.  Think "y-axis" (y goes up to the sky.)
Horizontal Line	<b>←</b>	A <b>horizontal</b> line goes from side to side, like the horizon.  Think " $x - axis$ "

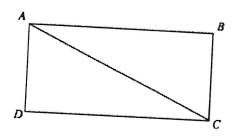
Type	Examples	Definition
Intersecting Lines		Intersecting lines are lines that cross each other.  Think of how streets cross each other at an intersection.
Parallel Lines		Parallel lines are two lines that are always the same distance apart.  They will never cross, or intersect, each other.  Think of railroad tracks.
Perpendicular Lines		Perpendicular lines are two intersecting lines that meet to form a right angle (90°).  Think of a capital or lower case" t" or the sign for time-out in sports.

1. Which street runs parallel to First Street?



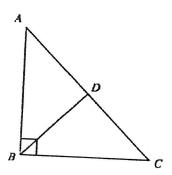
- A. Broadway
- B. Center Street
- C. Second Street
- D. Main Street

2. Which side of rectangle ABCD is parallel to  $\overline{AB}$ ?



- A.  $\overline{BC}$
- $B. \overline{CD}$
- $C. \overline{AD}$
- $D. \overline{AC}$

3. Which side of triangle ABC is perpendicular to  $\overline{AB}$ ?



- A.  $\overline{BD}$
- $B. \overline{AD}$
- $C. \overline{BC}$
- D. DC

4. Which illustration shows perpendicular lines?

A. X

В. //

 $C \rightarrow$ 

D. \_\_\_\_

# **Parallel Lines** Perpendicular Lines Draw a pair of parallel lines below using a Draw a pair of perpendicular lines below ruler. Your lines must be straight. using a ruler. Your lines must be straight. **Intersecting Lines** Right Angle Draw a pair of intersecting lines below Draw two rays that form a right angle. using a ruler. They should not be Your lines must be straight. perpendicular lines. Your lines must be straight.